

Algebra 1 – Chapter 5

Lesson 1

Name: Key

Date _____

Tell whether the ordered pair is a solution of the system of linear equations.

1. $(2, 6)$; $x + y = 8$

$3x - y = 0$

$2+6=8$

$8=8 \checkmark$

$3(2) - 6 = 0$

$6-6=0$

$0=0 \checkmark$

2. $(8, 2)$; $x - y = 6$

$2x - 10y = 4$

$8-2=6$

$6=6 \checkmark$

$2(8)-10(2)=4$

$16-20=-4$

$-4 \neq 4$

Yes!

No!

3. $(-4, -2)$; $y = 2x + 6$

$y = -3x - 14$

$-2=2(-4)+6$

$-2=-8+6$

$-2=-2 \checkmark$

$-2=3(-4)-14$

$-2=12-14$

$-2=-2 \checkmark$

Yes!

4. $(-2, 1)$; $6x + 5y = -7$

$2x - 4y = -8$

$6(-2)+5(1)=-7$

$-12+5=-7$

$-7=-7 \checkmark$

$2(-2)-4(1)=-8$

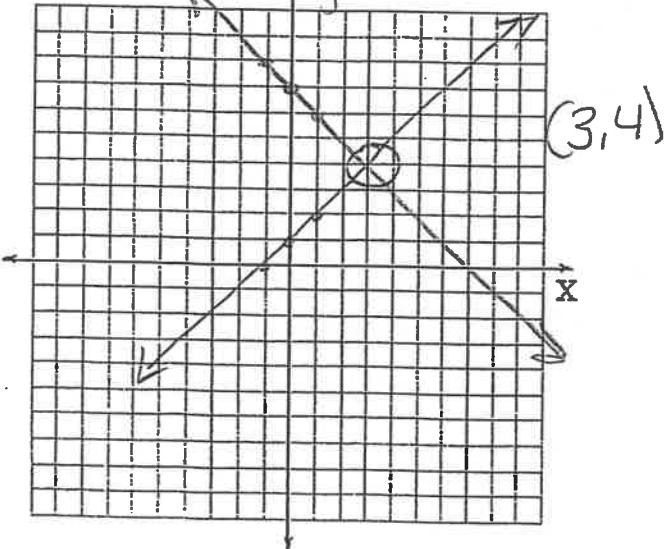
$-4-4=-8$

$-8=-8 \checkmark$

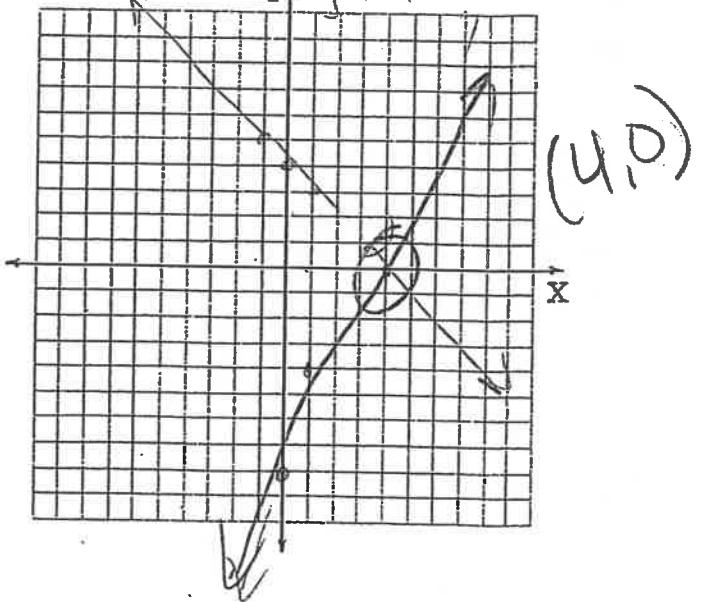
Yes!

Solve the system of linear equations by graphing.

5. $y = -x + 7$ Slope: -1
 $y = x + 1$ Y-int: 7
Slope: 1
Y-int: 1



6. $y = -x + 4$ Slope: -1
 $y = 2x - 8$ Y-int: 4
Slope: 2
Y-int: -8

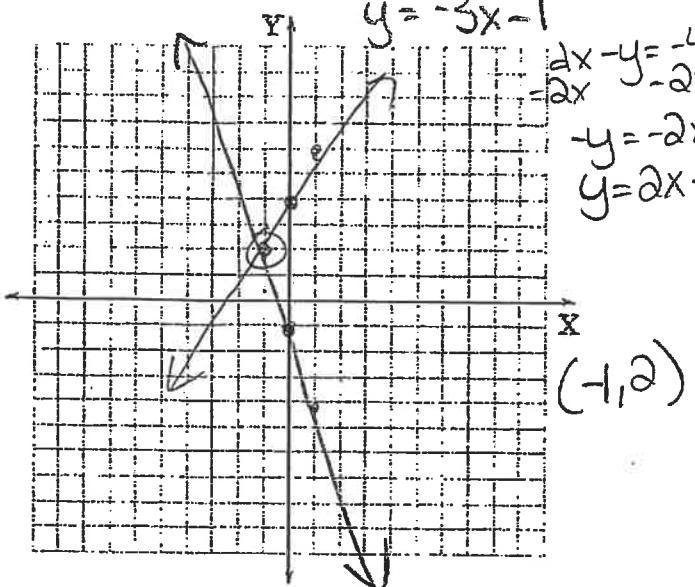


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Lesson 1

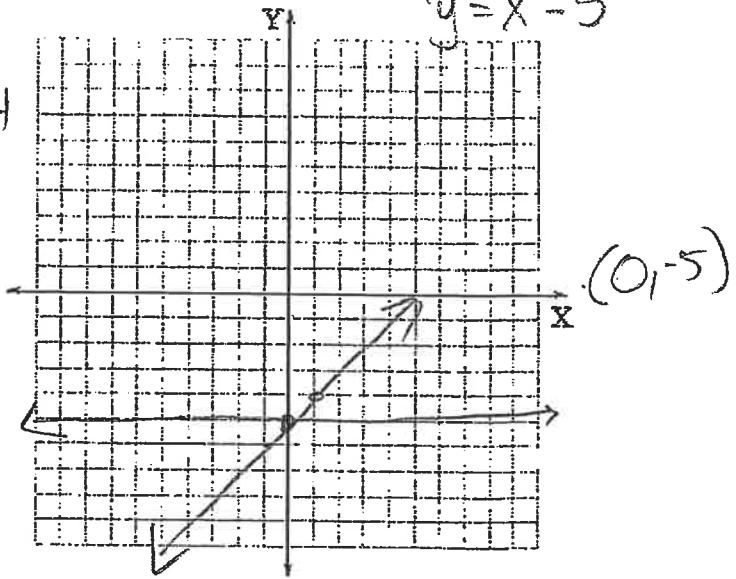
$$7. \begin{aligned} 9x + 3y &= -3 \\ 2x - y &= -4 \end{aligned}$$

$$\begin{aligned} 9x + 3y &= -3 \\ -9x &\quad -9x \\ 3y &= -9x - 3 \\ \frac{3y}{3} &= \frac{-9x}{3} - \frac{3}{3} \\ y &= -3x - 1 \end{aligned}$$

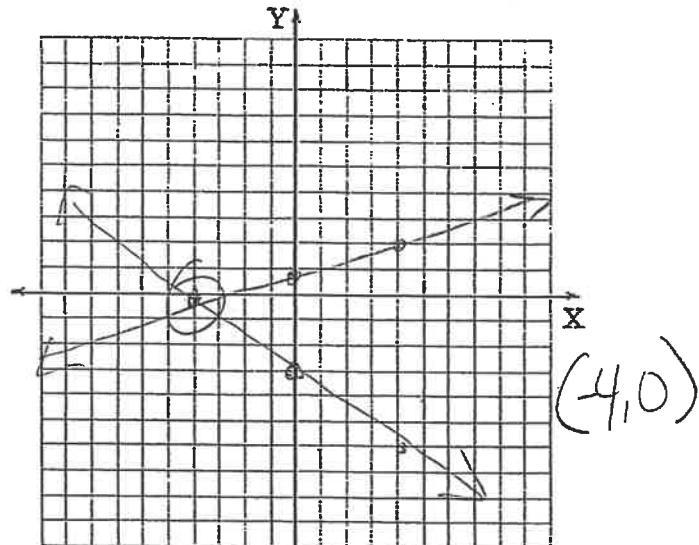


$$8. \begin{aligned} 4x - 4y &= 20 \\ y &= -5 \end{aligned}$$

$$\begin{aligned} 4x - 4y &= 20 \\ 4x &\quad -4x \\ -4y &= -4x + 20 \\ \frac{-4y}{-4} &= \frac{-4x}{-4} + \frac{20}{-4} \\ y &= x - 5 \end{aligned}$$



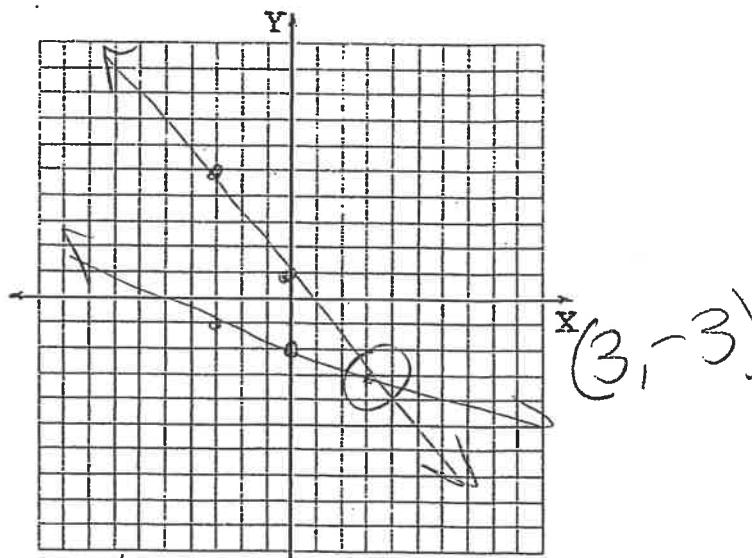
$$9. \begin{aligned} x - 4y &= -4 \\ -3x - 4y &= 12 \end{aligned}$$



$$\begin{aligned} x - 4y &= -4 \\ -x &\quad -x \\ -4y &= -x - 4 \\ \frac{-4y}{-4} &= \frac{-x}{-4} - \frac{4}{-4} \\ y &= \frac{1}{4}x + 1 \end{aligned}$$

$$\begin{aligned} -3x - 4y &= 12 \\ +3x &\quad +3x \\ -4y &= 3x + 12 \\ \frac{-4y}{-4} &= \frac{3x}{-4} + \frac{12}{-4} \\ y &= -\frac{3}{4}x - 3 \end{aligned}$$

$$10. \begin{aligned} 3y + 4x &= 3 \\ x + 3y &= -6 \end{aligned}$$



$$\begin{aligned} 3y + 4x &= 3 \\ -4x &\quad -4x \\ 3y &= -4x + 3 \\ \frac{3y}{3} &= \frac{-4x}{3} + \frac{3}{3} \\ y &= -\frac{4}{3}x + 1 \end{aligned}$$

$$\begin{aligned} x + 3y &= -6 \\ -x &\quad -x \\ 3y &= -x - 6 \\ \frac{3y}{3} &= \frac{-x}{3} - \frac{6}{3} \\ y &= -\frac{1}{3}x - 2 \end{aligned}$$

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Lesson 2

Name: Key

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Tell which equation you would choose to solve for one of the variables. Explain.

1. $x + 4y = 10$

$x - 2y = 0$

2. $3x - y = 0$

$2x + y = -10$

3. $5x + 3y = 11$

$5x - y = 5$

4. $3x - 2y = 19$

$x + y = 8$

(Solve the system of linear equations by substitution. Check your solution.

5. $x = 17 - 4y$

$y = x - 2$

$x = 17 - 4(x-2)$

$x = 17 - 4x + 8$

$x = 25 - 4x$
 $+4x \quad +4x$

$\frac{5x}{5} = \frac{33}{5}$

$x = 5$

$y = 5 - 2$

$y = 3$

$(5, 3)$

6. $6x - 9 = y$

$y = -3x$

$6x - 9 = -3x$

$-6x \quad -6x$

$\frac{-9}{-9} = \frac{-9x}{-9}$

$x = 1$

$y = -3(1)$

$y = -3$

$(1, -3)$

7. $x = 16 - 4y$

$3x + 4y = 8$

$3(16 - 4y) + 4y = 8$

$48 - 12y + 4y = 8$

$48 - 8y = 8$

$-48 \quad -48$

$\frac{-8y}{-8} = \frac{-40}{-8}$

$y = 5$

$x = 16 - 4(5)$

$x = 16 - 20$

$x = -4$

$(-4, 5)$

8. $-5x + 3y = 23$

$y = 10x - 8$

$-5x + 3(10x - 8) = 23$

$-5x + 30x - 24 = 23$

$25x - 24 = 23$

$+24 \quad +24$

$y = 10(4) - 8$

$y = \frac{98}{5} - \frac{40}{5}$

$25x = 47$

$(4, \frac{98}{5} - \frac{40}{5})$

$x = \frac{47}{25}$

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Lesson 2

Solve the system of linear equations by using substitution. Check your solution.

9. $5x + 2y = 9$

$$\begin{array}{r} x + y = -3 \\ -x \quad -x \end{array}$$

$$y = -x - 3$$

$$5x + 2(-x - 3) = 9$$

$$5x - 2x - 6 = 9$$

$$3x - 6 = 9$$

$$\begin{array}{r} 3x = 15 \\ \hline 3 \quad 3 \\ \boxed{x = 5} \end{array}$$

$$\begin{array}{r} 5+y = -3 \\ -5 \quad -5 \end{array}$$

$$y = -3$$

$$\begin{pmatrix} 5 & -3 \end{pmatrix}$$

10. $11x - 7y = -14$

$$\begin{array}{r} x - 2y = -4 \\ +2y \quad +2y \end{array}$$

$$x = 2y - 4$$

$$11(2y - 4) - 7y = -14$$

$$22y - 44 - 7y = -14$$

$$\begin{array}{r} 15y - 44 = -14 \\ +44 \quad +44 \end{array}$$

$$\frac{15y}{15} = \frac{30}{15}$$

$$y = 2$$

$$x + 2(2) = -4$$

$$x + 4 = -4$$

$$-4 \quad -4$$

$$x = -8$$

11. A farmer plants corn and wheat on a 180-acre farm. The farmer wants to plant three times as many acres of corn as wheat. Write a system of linear equations that represents this situation. How many acres of each crop should the farmer plant?

$$x = \text{corn}$$

$$y = \text{wheat}$$

$$x + y = 180$$

$$x = 3y$$

$$3y + y = 180$$

$$\frac{4y}{4} = \frac{180}{4}$$

$$y = 45$$

$$\cancel{x} = 3(45)$$

$$x = 135$$

12. A company that offers tubing trips down a river rents tubes for a person to use and "cooler" tubes to carry food and water. A group spends \$270 to rent a total of 15 tubes. Write a system of linear equations that represents this situation. How many of each type of tube does the group rent?

$$x = \text{tube}$$

$$y = \text{cooler}$$

$$x + y = 15$$

Typo - equation not finished

-Sorry! -

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Lesson 3

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Date _____

Solve the system of linear equations by elimination.

$$1. \begin{array}{l} x + 2y = 13 \\ -x + y = 5 \end{array}$$

$$\begin{array}{r} 3y = 18 \\ \hline 3 \\ y = 6 \end{array}$$

$$x + 2(6) = 13$$

$$\begin{array}{r} x + 12 = 13 \\ -12 -12 \end{array}$$

$$x = 1$$

$$(1, 6)$$

$$2. \begin{array}{l} 9x + y = 2 \\ -4x - x = -17 \end{array}$$

$$\begin{array}{r} 5x = -15 \\ \hline 5 \\ x = -3 \end{array}$$

$$9(-3) + y = 2$$

$$\begin{array}{r} -27 + y = 2 \\ +27 +27 \end{array}$$

$$y = 29$$

$$(-3, 29)$$

$$3. \begin{array}{l} -x + y = 4 \\ x + 3y = 4 \end{array}$$

$$\begin{array}{r} 4y = 8 \\ \hline 4 \\ y = 2 \end{array}$$

$$\begin{array}{r} -x + 2 = 4 \\ -2 -2 \end{array}$$

$$\begin{array}{r} -x = 2 \\ \hline -1 -1 \\ x = -2 \end{array}$$

$$x = -2$$

$$(-2, 2)$$

$$4. \begin{array}{l} 4x - 9y = -21 \\ -4x - 3y = 9 \end{array}$$

$$\begin{array}{r} -12y = -12 \\ \hline -12 \\ y = 1 \end{array}$$

$$4x - 9(1) = -21$$

$$\begin{array}{r} 4x - 9 = -21 \\ +9 +9 \end{array}$$

$$\begin{array}{r} 4x = -12 \\ \hline 4 \\ x = -3 \end{array}$$

$$(-3, 1)$$



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Lesson 3

Solve the system of linear equations by elimination.

5. $8x - 5y = 11$ $\rightarrow 8x - 5y = 11$
 $4x - 3y = 5 \quad \cancel{-2} \rightarrow -8x + 6y = -10$
 $y = 1$

$$8x - 5(1) = 11$$

$$8x - 5 = 11 \\ +5 \quad +5$$

$$\frac{8x}{8} = \frac{16}{8}$$

$$x = 2$$

$$\boxed{(2, 1)}$$

6. $10x - 9y = 46 \rightarrow 10x - 9y = 46$
 $-2x + 3y = 10 \quad \cancel{-5} \rightarrow -10x + 15y = 50$
 $\frac{6y}{6} = \frac{96}{6}$
 $y = 16$

$$10x - 9(16) = 46$$

$$10x - 144 = 46 \\ +144 \quad +144$$

$$\frac{10x}{10} = \frac{190}{10}$$

$$\boxed{(19, 16)}$$

$$x = 19$$

7. $-2x - 5y = 9 \quad \cancel{\cdot 3} \rightarrow -6x - 15y = 27$
 $3x + 11y = 4 \quad \cancel{\cdot 2} \rightarrow 6x + 22y = 8$
 $\underline{-15y = 35}$
 $y = 5$

$$-2x - 5(5) = 9$$

$$-2x - 25 = 9 \\ +25 \quad +25$$

$$\frac{-2x}{-2} = \frac{34}{-2}$$

$$x = -17$$

$$\boxed{(-17, 5)}$$

8. $12x - 7y = -2 \quad \cancel{\cdot 2} \rightarrow 24x + 14y = 4$
 $8x + 11y = 30 \quad \cancel{\cdot 3} \rightarrow 24x + 33y = 90$
 $\frac{47y}{47} = \frac{94}{47}$
 $y = 2$

$$12x - 7(2) = -2$$

$$12x - 14 = -2 \\ +14 \quad +14$$

$$\frac{12x}{12} = \frac{12}{12}$$

$$x = 1$$

$$\boxed{(1, 2)}$$

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Lesson 3

Solve the system of linear equations using any method. Explain why you chose the method.

9. $-6y + 2 = -4x$

$$\begin{array}{rcl} y - 2 & = & x \\ +2 & & +2 \end{array}$$

$$y = x + 2$$

$$-(4x+2) + 2 = -4x$$

$$-6x - 12 + 2 = -4x$$

$$-6x - 10 = -4x$$

$$+6x \qquad \qquad +6x$$

$$\frac{-10}{2} = \frac{2x}{2}$$

$$-5 = x$$

$$\begin{array}{rcl} y - 2 & = & -5 \\ +2 & & +2 \end{array}$$

$$y = -3$$

$$\boxed{(-5, -3)}$$

10. $3x + y = \frac{1}{3}$ $\xrightarrow{-3} 9x + 3y = \frac{3}{3}$
 $2x - 3y = \frac{8}{3}$ $\rightarrow 2x - 3y = \frac{8}{3}$

$$\begin{array}{rcl} 11x & = & \frac{11}{3} \\ 11 & & 11 \\ x & = & \frac{1}{3} \cdot \frac{1}{11} = \frac{1}{3} \\ x & = & \frac{1}{3} \end{array}$$

$$3\left(\frac{1}{3}\right) + y = \frac{1}{3}$$

$$1 + y = \frac{1}{3}$$

$$-1 \qquad \qquad -1$$

$$y = \frac{1}{3} - \frac{3}{3}$$

$$y = -\frac{2}{3}$$

$$\boxed{\left(\frac{1}{3}, -\frac{2}{3}\right)}$$

11. Solve for x , y , and z in the system of equations. Explain your steps.

$$x + 7y + 3z = 29$$

$$3z + x - 2y = -7$$

$$5y = 10 - 2x$$

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Lesson 4

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Solve the system of linear equations.

$$1. \ y = -2x - 4$$

$$y = 2x - 4$$

$$\begin{array}{r} 2x - 4 = -2x - 4 \\ +2x + 4 \quad +2x + 4 \\ \hline 4x = 0 \end{array}$$

$$x = 0$$

$$y = 2(0) - 4$$

$$y = -4$$

$$(0, -4)$$

$$2. \ y = -6x - 8$$

$$y = -6x + 8$$

$$\begin{array}{r} -6x + 8 = -6x - 8 \\ +6x \quad -8 \quad +6x - 8 \\ \hline 0 = -16 \end{array}$$

$$0 = -16$$

No Sol

$$3. \begin{array}{r} x + 2y = 7 \\ x - 2y = 7 \\ \hline 0 = 7 \end{array}$$

$$0 = 7$$

No Sol

$$4. \begin{array}{r} 3x - y = 6 \\ -3x + y = -6 \\ \hline 0 = 0 \end{array}$$

$$0 = 0$$

Inf Many

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Lesson 4

$$5. \begin{aligned} 4x + 4y &= -8 \\ -2x - 2y &= 4 \end{aligned} \rightarrow \begin{aligned} 4x + 4y &= -8 \\ -4x - 4y &= -8 \end{aligned} \rightarrow \underline{0 = 0}$$

Inf. Many

$$6. \begin{aligned} 15x - 5y &= -20 \\ -3x + y &= 4 \end{aligned} \rightarrow \begin{aligned} 15x - 5y &= -20 \\ -15x + 5y &= 20 \end{aligned} \rightarrow \underline{0 = 0}$$

Inf. Many

Use only slopes and y-intercepts of the graphs of the equations to determine whether the system of linear equations has one solution, no solutions, or infinitely many solutions. Explain.

$$7. \begin{aligned} y &= 7x + 13 \\ -21x + 3y &= 39 \end{aligned}$$

$$+21x \quad +21x$$

$$\frac{3y}{3} = \frac{21x + 39}{3}$$

$$y = 7x + 13$$

Slopes: $7x + 7x$

y-int: $13 + 13$

Inf. Many

$$8. \begin{aligned} y &= -6x - 2 \\ 12x + 2y &= -6 \end{aligned}$$

$$-12x \quad -12x$$

$$\frac{2y}{2} = \frac{-12x - 6}{2}$$

$$y = -6x - 3$$

Slopes: $-6 + -6$

y-int: $-2 + -3$

No Sol | Same slope
differently-int

$$9. \begin{aligned} 4x + 3y &= 27 \\ 4x - 3y &= -27 \end{aligned}$$

$$\begin{aligned} 4x + 3y &= 27 \\ -4x & \quad -4x \end{aligned} \quad \begin{aligned} 4x - 3y &= -27 \\ -4x & \quad -4x \end{aligned}$$

$$\frac{3y}{3} = \frac{-4x + 27}{3}$$

$$y = -\frac{4}{3}x + 9$$

$$-\frac{3y}{3} = \frac{4x - 27}{3}$$

$$y = \frac{4}{3}x - 9$$

One Sol

$$10. \begin{aligned} 2x - 2y &= 16 \\ 3x - 6y &= 30 \end{aligned}$$

$$\begin{aligned} 2x - 2y &= 16 \\ -3x & \quad -3x \end{aligned}$$

$$-\frac{2y}{2} = \frac{-2x + 16}{2}$$

$$y = x - 8$$

$$\begin{aligned} 3x - 6y &= 30 \\ -3x & \quad -3x \end{aligned}$$

$$-\frac{6y}{6} = \frac{3x + 30}{6}$$

$$y = \frac{1}{2}x - 5$$

One Solution

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Lesson 7

Name: Key

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Tell whether the ordered pair is a solution of the system of linear inequalities.

1. $(-4, 3)$

No

2. $(-3, -1)$

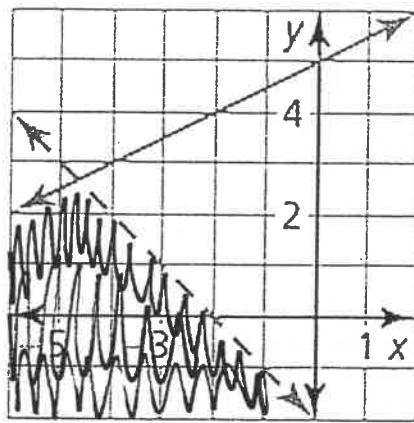
No

3. $(-2, 5)$

No

4. $(1, 1)$

No



Tell whether the ordered pair is a solution of the system of linear inequalities.

5. $(-5, 2)$: $y < 4$

$y > x + 3$

$$\begin{array}{ll} y < 4 & y > x + 3 \\ 2 < 4 \checkmark & 2 > -5 + 3 \\ 2 > -2 \checkmark \end{array}$$

Yes!

6. $(1, -1)$: $y > -2$

$y > x - 5$

$$\begin{array}{ll} y > -2 & y > x - 5 \\ -1 > -2 \checkmark & -1 > 1 - 5 \\ & -1 > -4 \checkmark \end{array}$$

Yes!

7. $(0, 0)$: $y \leq x + 7$

$y \geq 2x + 3$

$$\begin{array}{ll} y \leq x + 7 & y \geq 2x + 3 \\ 0 \leq 0 + 7 & 0 \geq 2(0) + 3 \\ 0 \leq 7 \checkmark & 0 \geq 3 \end{array}$$

No

No!

8. $(4, -3)$: $y \leq -x + 1$

$y \leq 5x - 2$

$$\begin{array}{ll} y \leq -x + 1 & y \leq 5x - 2 \\ -3 \leq -4 + 1 & -3 \leq 5(4) - 2 \\ -3 \leq -3 \checkmark & -3 \leq 20 - 2 \\ & -3 \leq 18 \end{array}$$

No

No!

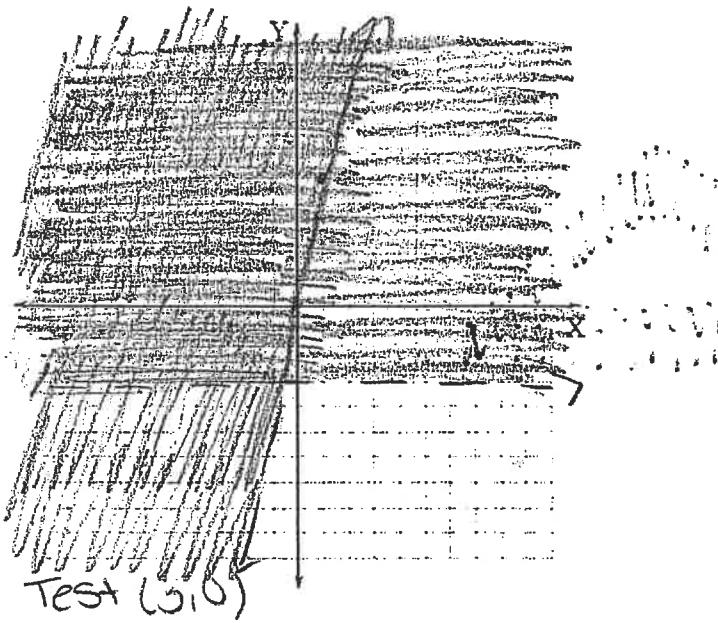
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Lesson 7

Graph the system of linear inequalities.

9. $y > -3$

$y \geq 5x$



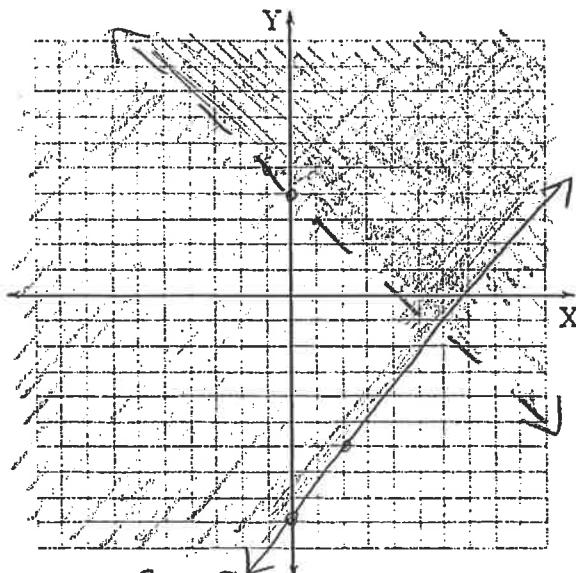
Test (3, 0)

$0 \geq 5(3)$

$0 \geq 15$

No!

$$11. \begin{aligned} x + y &> 4 & x+y &> 4 & \text{Test } (0, 0) \\ y &\geq \frac{3}{2}x - 9 & -x & y &\geq -x + 4 & 0+0 &> 4 \\ && y && & 0 &> 4 \\ && && & \text{No} \end{aligned}$$



$y \geq \frac{3}{2}x - 9$

Test (0, 0)

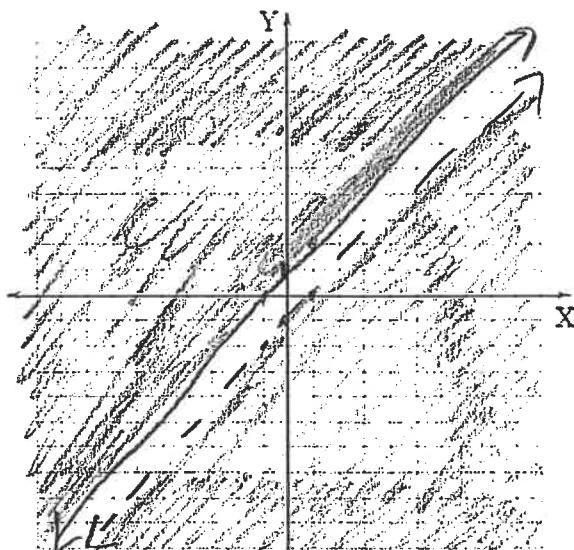
$0 \geq \frac{3}{2}(0) - 9$

$0 \geq -9$

Yes!

10. $y < x - 1$
 $y \geq x + 1$

Test (0, 2)
 $2 < 0 - 1$ No
 $2 \geq 0 + 1$ Yes



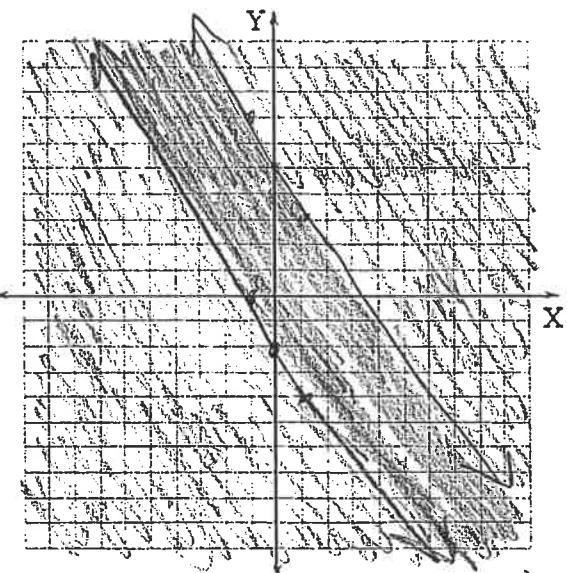
Test (1, 0)

$0 > 1 - 1$

$0 \geq 2$ No

No Solution

12. $2x + y \leq 5$ $\frac{\partial x + y \leq 5}{\partial x}$ Test (0, 0)
 $y + 2 \geq -2x$ $y \leq -2x + 5$ $\frac{\partial(0) + (0) \leq 5}{0 \leq 5}$



$y + 2 \geq -2x$
 $-2 \geq -2$

Test (0, 0)

$0 + 2 \geq -2(0)$

$y \geq -2x - 2$
 $0 \geq 0$

Yes